

3 **Household slow sand filters operating in continuous and intermittent flows:**  
4 **computational fluid dynamics simulation and validation by tracer experiments**

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20  
21 **Abstract**

22 This paper analysed geometries and flows in household slow sand filters (HSSFs)  
23 through computational fluid dynamics (CFD) to evaluate the hydrodynamics of filters.  
24 Four HSSFs in full scale were studied with a capacity to produce 48 L.d<sup>-1</sup> each with  
25 diameters of 190 mm and 250 mm and with a filter medium depth of 0.5 meters. The

26 hydrodynamics of the four mathematical models of the HSSFs was validated using the  
27 experimental residence time distribution (RTD). The Kruskal Wallis non-parametric test  
28 indicates that the results of the experimental RTDs and the simulated RTDs did not  
29 show significant differences, therefore the mathematical models represent the physical  
30 models, which requires a detailed 3D analysis of the flow in the filters. The results  
31 showed that the HSSFs have a flow close to plug flow reactor. Internal recirculation  
32 zones were not found, nor short-circuit ones; however, dead zones were verified at the  
33 base of the filter with volumes below 3% when compared to the total volume of the  
34 filtering and draining layers, not necessary to make changes in geometry. The results of  
35 the computational simulation showed that the continuous filters had a smaller velocity  
36 variation and the filters with smaller diameter presented a reduction in dead zones when  
37 compared to the filters with larger diameters operated in the same flow regime. The  
38 study focused on the hydraulic aspects of HSSFs, but it is noteworthy that the choice of  
39 the type of operation to be adopted by families that use this type of treatment depends  
40 on studies that assess the efficiency of water treatment filters that were not considered in  
41 this work.

42

43 **Keywords:** biosand filter, computational fluid dynamics (CFD); drinking water;  
44 residence time distribution (RTD); software *ANSYS Fluent*

45

## 46 **1. Introduction**

47 The ingestion of water contaminated by feces, the lack of collection and  
48 treatment of sanitary sewage and inadequate hygiene habits are the causes of about 4  
49 billion diarrheal diseases per year, and out of these 1.8 million are fatal (UNEP, 2016).  
50 According to Dadonaite et al. (2020), in 2016, it was estimated that 1.55 million deaths

51 were caused by diarrheal diseases worldwide and, in 2017, that number increased to 1.6  
52 million; one third of whom were children under the age of five.

53 An inexpensive and efficient way to empower people without access to water,  
54 both in urban and rural areas that are not provided with a distribution network, is to use  
55 the so-called point-of-use treatment technologies (POU) and, among them, Household  
56 Slow Sand Filters (HSSFs) can be highlighted (Sobsey et al., 2008).

57

### 58 **1.1. Features and functioning of HSSFs**

59 HSSFs were adapted from conventional slow sand filters (SSFs) designed to  
60 operate in batch. Both the HSSF and the SSF allow the development of a biological  
61 layer on top of the granular medium that helps the treatment (CAWST, 2012; Maciel  
62 and Sabogal-Paz, 2020; Andreoli and Sabogal-Paz, 2020).

63 Research carried out on HSSFs showed how easy it is for a user to construct and  
64 operate them. These studies focus on evaluating the efficiency (Kennedy et al., 2012;  
65 Maciel and Sabogal-Paz, 2020; Terin and Sabogal-Paz, 2019; Sabogal-Paz et al 2020;  
66 Andreoli and Sabogal-Paz, 2020).

67 The fundamentals of HSSF contaminant removal are the combination of  
68 physical and biological processes. According to Jadhav, Husain and Chavan (2015),  
69 physical mechanisms include retention of particles in the pores of the filter media and  
70 an adsorption, which allows for organic removal, while biological components include  
71 predation, elimination, natural death/inactivation and partial reduction of organic carbon  
72 due to the metabolism of the microorganism. Therefore, the HSSF treats water by a  
73 combination of physical processes with biological activity present on the surface of the  
74 filter layer (*schmutzdecke*).

75           The I-HSSF can operate with a filtration rate of up to  $26.4 \text{ m}^3 \cdot \text{m}^{-2} \cdot \text{day}^{-1}$  (Elliot et  
76 al., 2006) and the recommended pause period is in the range of 1 to 48 hours (Cawst,  
77 2012).

78           The continuous flow filter (C-HSSF) can be operated with a lower filtration rate,  
79 up to  $9.6 \text{ m}^3 \cdot \text{m}^{-2} \cdot \text{day}^{-1}$  (Maciel and Sabogal-Paz, 2020) and its feeding can be by gravity  
80 or direct pumping, if there is a control of the filtration rate (Sabogal-Paz et al., 2020).

81           In the intermittent flow filter (I-HSSF), the water to be treated must be  
82 maintained in the filter medium pores between each batch feed, generating the pause  
83 period that is important as it allows physical and biological processes to occur to treat  
84 water (Sabogal-Paz et al 2020). The study developed by Elliott et al. (2008) showed that  
85 the best filter performance occurs when the volume of water to be treated is close to the  
86 pore volume.

87           In the study by Maciel and Sabogal-Paz (2020), continuous filters operated at a  
88 filtration rate of  $0.68 \text{ m}^3 \cdot \text{m}^2 \cdot \text{day}^{-1}$  obtained residence time distribution (RTDs) of 991  
89 min. and 876 min. with a turbidity reduction of 89.4% and 83.8%, respectively, and the  
90 intermittent filters showed turbidity removal of 91.8 and 90.5%. Terin and Sabogal-Paz  
91 (2019) worked with HSSF operating in continuous flow at a filtration rate of  $1.22$   
92  $\text{m}^3 \cdot \text{m}^2 \cdot \text{day}^{-1}$ . and obtained a turbidity reduction of 84.39% for the RTD 417 min. and the  
93 filter intermittent showed a reduction in turbidity of 81.41% for the 4-hour pause period  
94 and 83.78% for the 12-hour pause period.

95           The C-HSSF was classified as a piston flow reactor by Maciel and Sabogal-Paz  
96 (2018), Sabogal-Paz et al. (2020), Terin and Sabogal-Paz (2019) and Young-Rojanschi  
97 and Madramootoo (2014b), there is a gap in these studies in terms of not analyzing the  
98 influence of possible short circuits and dead zones on residence time and quality of

99 water. This question was addressed in the present study using the CFD to analyze the  
100 DTR, the type of flow and possible short-circuit influences and dead zones.

101

## 102 **1.2. Tracer test**

103 The simplest and most direct way to determine the residence time distribution  
104 (RTD) is to use a non-reactive tracer, using the stimulus and response technique.  
105 Various types of experiments can be used with pulse and/or step type stimuli  
106 (Levenspiel, 1999).

107 In real chemical reactors, in general, they tend to deviate from ideality, but for  
108 the hydrodynamic characterization of reactors the ideal flows are considered for  
109 modelling, which are: Plug Flow Reactor - (PFR) and Continuous Stirred Tank Reactor  
110 – (CSTR) (Levenspiel, 1999). In the studies by Andreoli and Sabogal-Paz (2020),  
111 Bradley et al. (2011), Elliott et al. (2008), Maciel and Sabogal-Paz (2020), Lynn et al.  
112 (2013), Sabogal-Paz et al. (2020) and Terin and Sabogal-Paz (2019), the hydraulic  
113 behaviour of the I-HSSF was evaluated and classified as a plug flow reactor. The C-  
114 HSSF was also classified as a plug flow reactor by Maciel and Sabogal-Paz (2020),  
115 Sabogal-Paz et al. (2020), Terin and Sabogal-Paz (2019), Young-Rojanschi and  
116 Madramootoo (2014a).

117 The necessary condition for plug flow reactors is that the residence time must be  
118 the same for all fluid elements (Levenspiel, 1999). Thus, the fluid passes through the  
119 filter without mixing the fluid from the front and back inlet, that is, without  
120 overflowing. It should be noted that in a plug flow reactor, the composition of the fluid  
121 varies from point to point along a flow path (Levenspiel, 1999). In this context, Elliott  
122 et al. (2008) evaluated an HSSF that showed a minimal effect of dispersion by flow  
123 paths through porous media. Therefore, the microbial removal process occurs

124 homogeneously in all water portions that enter the HSSF and advance with the depth in  
125 the biological layer (Sabogal-Paz et al., 2020).

126

### 127 **1.3. Mathematical modelling and simulation of HSSFs**

128 Mathematical models can predict results from the control and operating  
129 conditions defined by users to foresee improvements in a filtration process when  
130 producing drinking water (Botari and Di Bernardo, 2012). The mathematical models  
131 used in the CFD are obtained through differential or integral balances of the conserved  
132 properties, that is, they adopt the principles of conservation of mass, momentum and  
133 energy.

134 The CFD has become a robust tool in the reactor design and diagnosis process,  
135 providing detailed information about the reactors, such as the velocity distribution field,  
136 the concentration distribution and energy consumption (Zhang et al., 2007).

137 According to Langergraber et al. (2009), mathematical models were developed  
138 and validated with experimental tests, thus they can be used to evaluate and improve  
139 existing design criteria. The CFD is normally used in the tracer test simulation and  
140 validated with the physical experiment tracer test (Brannock et al., 2010; Furman and  
141 Stegowski, 2011; Gharibian et al., 2020; Klusener et al., 2007; Qi et al., 2013; Zhang et  
142 al., 2007).

143

### 144 **1.4. Tracer test with CFD**

145 The comparison of the experimental RTD with the CFD by RTD prediction is  
146 essential to ensure an acceptable precision of the mathematical model (Furman and  
147 Stegowski, 2011).

148           Regarding the application of the RTD technique to filters, Qi et al. (2013)  
149 performed tracer tests with CFD in an upstream sand filter with a length of 2.0 m and  
150 width 1.0 m and flow rate of 25.2 L.h<sup>-1</sup> and determined the RTD to characterize the flow  
151 in filters with two configurations, which are: the first, without a support layer, without a  
152 layer of water on the filter layer and with a collector tube along the entire length in the  
153 upper portion of the filter layer; and the second, with a support layer, with a layer of  
154 water on the filter layer and with a collector tube in part of the upper portion of the filter  
155 layer.

156           The CFD simulation, developed by Qi et al. (2013), indicated that the water  
157 current lines had an upward and downward sloping direction, and the velocity in the  
158 middle of the filter was the highest; about five times greater than the minimum. The  
159 comparison of the experimental results with the CFD simulation concludes that the filter  
160 that had the support layer, the water slide and partial collector tube eliminated the  
161 preferred paths and the stagnation zones compared to the filter that did not have these  
162 characteristics. In filters with preferential flow paths, it was proven that the RTD  
163 obtained with CFD was lower than the calculated RTD.

164           Although there is research on the hydrodynamics of HSSFs, little has been  
165 discussed about the influence of the outlet system on the hydrodynamics of filters  
166 (Berbert et al., 2016). The study by Berbert et al. (2016) consisted of analysing the  
167 influence of the HSSF output system on the hydrodynamics of the filters and three  
168 different models operated in intermittent flow were simulated in the ANSYS-CFX  
169 software: the PEU/ UEM model (Berbert et al., 2016), the CAWST version 10  
170 (CAWST, 2012) and HydrAid (Kikkawa, 2008).

171           The filters of the CAWST and HydrAid models were simulated with the original  
172 geometry that has an outlet system on the side and an outlet configuration with a

173 collector ring inside was simulated. In the PEU/UEM model, four types of localized  
174 outlets were simulated: in the center in an upward flow, on the side, at the bottom and a  
175 collector ring inside. The study concluded that the PEU/UEM filter that has a collector  
176 ring-shaped output with the interface downwards contributes to improving the current  
177 lines by creating a better distribution of velocity across the three axes, reducing dead  
178 zones and increasing hydraulic residence time (Berbert et al., 2016).

179

## 180 **2. Materials and methods**

### 181 **2.1 Experimental**

#### 182 **2.1.1 Construction and operation of HSSFs**

183 Four HSSFs were evaluated, two in continuous flow (C-HSSFs) and two in  
184 intermittent flow (I-HSSFs). The filters were built with four layers of the same  
185 thickness composed of fine sand, coarse sand, fine gravel and coarse gravel, and above  
186 the fine sand there was a water slide, which is presented in detail in the supplementary  
187 material. The maximum water level above the filter layer was regulated by a float valve.

188 The C-HSSF1 was a continuous flow filter built in acrylic with a diameter of  
189 190 mm and the C-HSSF2, which was also operated in continuous flow, however it was  
190 built in PVC with a diameter of 250 mm. The I-HSSF1 operated in an intermittent flow  
191 with a 190 mm diameter acrylic body and the I-HSSF2 had the same flow as the  
192 previous one, but it was built in PVC with a diameter of 250 mm. Filters with a  
193 diameter of 190 mm had a cross-sectional area of  $0.028 \text{ m}^2$  and filters with a diameter of  
194 250 mm had a cross-sectional area of  $0.049 \text{ m}^2$ . The base of the HSSFs consisted of a  
195 CAP-type connection, and in the center of that base an outlet tube (collector) was fitted  
196 with a tap to capture the filtered water.

197 The walls of C-HSSF1 and I-HSSF1 were covered to prevent algae proliferation  
198 inside by sunlight entering through the acrylic material. The filtration rate of continuous  
199 filters was  $1.69 \pm 0.01 \text{ m}^3 \cdot \text{m}^{-2} \cdot \text{day}^{-1}$  for C-HSSF1 and  $0.97 \pm 0.96 \text{ m}^3 \cdot \text{m}^{-2} \cdot \text{day}^{-1}$  for C-  
200 HSSF2. On the other hand, the I-HSSF hydraulic head was variable and, consequently,  
201 the filtration rate as well. The maximum filtration rate of I-HSSF1 was  $3.2 \text{ m}^3 \cdot \text{m}^{-2} \cdot \text{day}^{-1}$   
202 shortly after feeding and decreased to zero and the maximum filtration rate of I-HSSF2  
203 was  $3.94 \text{ m}^3 \cdot \text{m}^{-2} \cdot \text{day}^{-1}$ . The filters had a daily production of 48 L each.

204

### 205 **2.1.2 Physical characterization of materials**

206 The thickness of the water layers (top of fine sand), fine sand, coarse sand, fine  
207 gravel and coarse gravel, respectively, were 10 cm, 50 cm, 5 cm, 5 cm and 7.5 cm. The  
208 fine sand had an equivalent diameter of 0.17 mm ( $D_{10}$ ), a uniformity coefficient of 1.73  
209 average particle diameter of  $2.70 \times 10^{-4}$  m. The physical parameters used in the study,  
210 such as: the thickness of the layers, granulometry, specific mass, the void index and the  
211 permeability were the same for the four filters and the standards used in the tests are  
212 contained in the supplementary material.

213

### 214 **2.1.3 Experimental RTD**

215 The disturbance chosen for C-HSSFs and I-HSSFs was of the step type, as  
216 reported by Maciel and Sabogal-Paz (2020), Terin and Sabogal-Paz (2019) and  
217 Sabogal-Paz et al (2020).

218 Tracer tests on each of the filters were performed in triplicate with a sodium  
219 chloride solution with a concentration of  $100 \text{ mg} \cdot \text{L}^{-1}$ . The variation in the electrical  
220 conductivity of the filtered water was measured at the filter outlet, in real time, with a  
221 conductivity probe from Venier Software & Technology, USA.

222           The conductivity probe was positioned at the outlet of the tap and inside a bottle.  
223 This bottle made it possible to read the samples as the treated water that came out  
224 through the tap was collected and temporarily stored in that bottle and renewed each  
225 time a new sample of treated water was received.

226           The calibration of the probe allowed to correlate the variation in conductivity  
227 with the concentration of the tracer. The probe was connected to a computer with the  
228 Logger Lite software (Venier Software & Technology, USA) that allowed us to collect  
229 and store the data of the measurements of the tracer concentration over time. The  
230 dynamic response time of the conductivity probe was 5 seconds and the data were  
231 measured every 60 s in the treated water that was collected at the filter outlet.

232           Data processing was performed using Excel 2013 software (Microsoft®, USA)  
233 and OriginPro 8 software (OriginLab, USA). The concentration versus time curve was  
234 normalized to obtain the F curve and then derived to obtain the E curve. After each test,  
235 the filters were cleaned by introducing tap water until the tracer was completely  
236 eliminated.

237           In the C-HSSFs, the tracer tests were performed with the same filtration rate  
238 used during the operation of the filters. The procedure resulted in the concentration  
239 versus time curve (C vs. t). These experimental curves were adjusted based on the three  
240 mathematical models of dispersion: model of continuous mixing tank reactors (N-  
241 CSTRs) and the models of low and high dispersion, as reported by Levenspiel (1999).

242           In the I-HSSFs tracer tests, the disturbance was performed with the first feeding  
243 with  $100 \text{ mg.L}^{-1}$  salt solution and then with tap water until the tracer concentration was  
244 close to zero. The filtration rate decreased to zero when the hydraulic load reached the  
245 minimum water level, at which time new feeding was performed. The volume of each

246 feed corresponded to the volume of voids in the filter. In total, four 10 L feeds were  
247 used in I-HSSF1 and four 15 L feeds in I-HSSF2.

248         Afterwards, the Modified Morris Dispersion Index (MMDI) proposed by Lynn  
249 et al. (2013) was calculated, which is a modification of the Morrill Dispersion Index  
250 (MDI) according to Tchobanoglous et al. (2003). The MDI index ranges from 1.0 (ideal  
251 piston flow reactors - PFR) to 22 (ideal complete mix reactors - CSTR) according to  
252 Tchobanoglous et al. (2003).

253         The theoretical RTD was calculated considering the ratio between the volume of  
254 water stored by C-HSSF1 and C-HSSF2 of 10L and 15L, respectively, and the daily  
255 flow of 48 L for both.

256

## 257 **2.2. Mathematical modelling and simulation of HSSFs**

258         The simulations of the HSSFs solved the mass conservation and momentum  
259 conservation equations using the ANSYS Fluent software (version 2020 R2) based on  
260 the finite volume method, where the differential equations are integrated in each mesh  
261 control volume, generating a set of discrete algebraic equations. The resulting linear  
262 system was then solved numerically in an iterative way until the solution was reached  
263 with previously determined precision.

264         The three-dimensional equations of the conservation of mass and amount of  
265 movement are given by Eq. 1 (all domains - continuity equation) and Eq. 2 (fluid  
266 domain - Navier-Stokes equation) (Navier, 1823; Stokes, 1845). In the filtering and  
267 support layers of the HSSFs, the term source of moment ( $S_i$ ) was added to the fluid flow  
268 equations in Eq. 3 (Porous Domain, simple homogeneous porous media of Darcy-  
269 Forchheimer Equation) (Darcy, 1856; Forchheimer, 1901a, 1901b). The term source of  
270 moment consists of two parts: loss of viscosity (i.e., Darcy's Law in porous media, the

271 first term on the right side of Eq. 3), and inertial loss (i.e., the second term on the right  
 272 side of Eq. 3).

$$273 \quad \nabla \cdot (\rho u) = 0 \quad (1)$$

$$\nabla \cdot (\rho u) = 0$$

$$274 \quad \nabla \cdot (\rho u u) = -\nabla p + \nabla \cdot \left( \mu (\nabla u + \nabla u^T) - \frac{2}{3} \delta \nabla \cdot u \right) \quad (2)$$

$$\nabla \cdot (\rho u u) = -\nabla p + \nabla \cdot \left( \mu (\nabla u + \nabla u^T) - \frac{2}{3} \delta \nabla \cdot u \right)$$

$$275 \quad S_i = - \left( \frac{\mu}{\alpha} u_i + C_2 \frac{1}{2} \rho |u| u_i \right) \quad (3)$$

$$S_i = - \left( \frac{\mu}{\alpha} u_i + C_2 \frac{1}{2} \rho |u| u_i \right)$$

276

277 Where,  $u \in \mathbb{R}^3$  is the velocity vector;  $\rho$  is the density of the fluid (water) [kg.m<sup>-3</sup>];  
 278  $p$  is the pressure [atm];  $\mu$  is the viscosity [m<sup>2</sup>.s<sup>-1</sup>]; where,  $S_i$  is the source term for  $i$  in  
 279 ( $x$ ,  $y$  or  $z$ ) in the moment equation,  $\alpha$  is the permeability of the porous medium [cm.s<sup>-1</sup>],  
 280  $|u|$  is the magnitude of the velocity [m.s<sup>-1</sup>], and  $D$  and  $C$  are the diagonal matrices  
 281 with  $1/\alpha$  and  $C_2$ , respectively.

282 Eq. 3 contributes to the pressure gradient in the porous cell, creating a pressure  
 283 reduction that is proportional to the velocity of the fluid in the cell (ANSYS, 2013). The  
 284 parameters of viscous resistance ( $1/\alpha$ ) and inertial resistance ( $C_2$ ) used for porous media  
 285 are calculated by Eq. 4 and Eq. 5 of the Ergun Equation (Ergun, 1952).

$$286 \quad \alpha = \frac{D_p^2}{150} \cdot \frac{\varepsilon^3}{(1 - \varepsilon)^2} \quad (4)$$

$$\alpha = \frac{D_p^2}{150} \cdot \frac{\varepsilon^3}{(1 - \varepsilon)^2}$$

$$287 \quad C_2 = \frac{3,5}{D_p} \cdot \frac{(1 - \varepsilon)}{\varepsilon^3} \quad (5)$$

$$C_2 = \frac{3,5}{D_p} \cdot \frac{(1 - \varepsilon)}{\varepsilon^3}$$

288 Where:  $1/\alpha$  – Viscous resistance [ $\text{m}^2$ ];  $D_p$  - Average particle diameter [m];  $\varepsilon$  –  
 289 Index of voids [ $\text{kg}\cdot\text{m}^{-3}\cdot\text{kg}^{-1}\cdot\text{m}^3$ ];  $C_2$  – Inertial resistance [ $\text{m}^{-1}$ ];  $\varepsilon$  – Fraction of voids  
 290 [ $\text{kg}\cdot\text{m}^{-3}\cdot\text{kg}^{-1}\cdot\text{m}^3$ ].

291 In laminar flows through porous media, the pressure drop is typically  
 292 proportional to the velocity and the constant  $C_2$  can be considered zero (ANSYS, 2013).  
 293 Ignoring convective acceleration and diffusion, the middle model is reduced to Darcy's  
 294 Law (Darcy, 1856), according to Eq. 6.

295 (6)

$$\nabla p = -\frac{\mu}{\alpha} u$$

296 Inertial losses in a porous medium, at high flow velocities, can be corrected by  
 297 the constant  $C_2$  of Eq. 3. This constant can be seen as a loss coefficient per unit length  
 298 along the flow direction, thus allowing the drop of pressure, specified as a function.

299 If the permeability term can be eliminated, only the term of inertial loss can be  
 300 used, producing the simplified form of the porous medium equation (Eq. 3) by Eq. 7 in  
 301 the x, y and z directions (ANSYS, 2013).

302 (7)

$$\nabla p = -\sum_{j=1}^3 C_{2ij} \left( \frac{1}{2} \rho \mathbf{u} |\mathbf{u}| \right)$$

303

304 The physical domain to be studied in the HSSFs is delineated by the walls of the  
 305 filter and its interior, composed of layers of water, filter material and the support layer.  
 306 The physical properties of the constituent materials of the physical domain, such as  
 307 viscosity, specific mass, pressure, porosity and hydraulic conductivity (or permeability),  
 308 were obtained in laboratory tests (supplementary material). The viscosity used was  
 309  $1.003 \times 10^{-3} \text{ kg}\cdot\text{m}^{-1}\cdot\text{s}^{-1}$  and the density was  $9.982 \times 10^2 \text{ kg}\cdot\text{m}^{-3}$ .

310 Thus, the boundary conditions of entry and exit were established for each of the  
311 constituent layers of the HSSF and the behaviour of the solution of the equations as a  
312 function of time was specified.

313 The CFD simulation was developed using Ansys 2020 R2 software from  
314 Ansys® and its subcomponents and a model was generated for each filter. Initially, the  
315 geometry of each HSSF was created using Autodesk® AutoCAD 2010®, and then the  
316 mesh was generated using Ansys 2020 R2 Meshing (Ansys®) with different refinements.  
317 Then, the control conditions were defined to run the simulation in Ansys 2020 R2  
318 Fluent (Ansys®) and the results were visualized in Ansys 2020 R2 CFD Post (Ansys®).

319 The models were simulated on a computer with an Intel® Core™ i7-7500U  
320 CPU @ 2.70 GHz 2.90 GHz, 64-bit operating system, 8 GB installed memory (RAM), 1  
321 TB HD, operating on Microsoft's Windows 10 platform®.

322 The results generated the velocity profiles and the flow current lines inside the  
323 filters. At the end of the simulation, the verification and validation of the mathematical  
324 models were performed based on the results obtained in the experimental tracer tests.

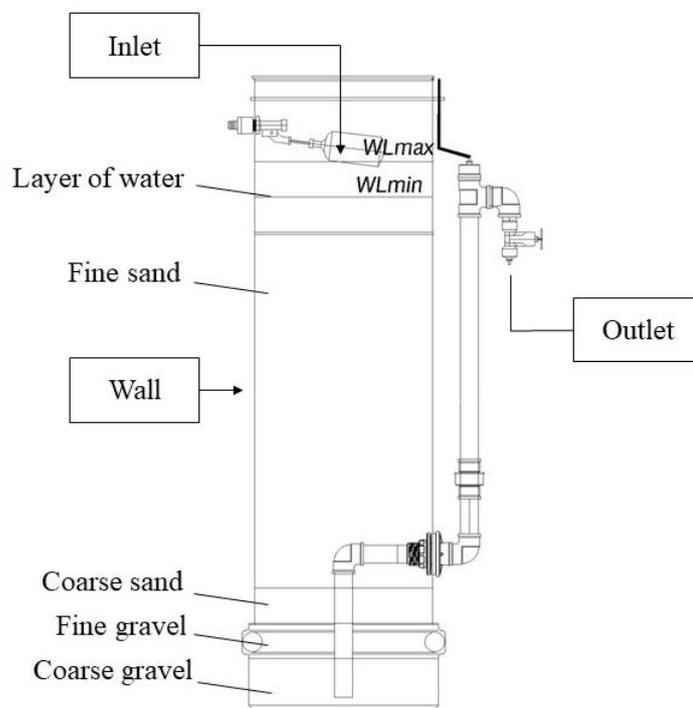
325 In the present study, two simulations were carried out for each HSSF: the first of  
326 the flow, which was carried out in a permanent regime; and the second from RTD,  
327 performed in a transient regime (passive scalar).

328 In the four mathematical models of the HSSFs, to facilitate modelling, the  
329 following criteria were adopted: i) single-phase flow in three dimensions; ii) Newtonian  
330 fluid at steady state; iii) isothermal flow, laminar flow, incompressible flow and flow in  
331 porous medium in the filtering and draining layers; and iv) homogeneous and specific  
332 porosity and permeability for each of the filtering and draining layers; as reported by  
333 Berbert et al. (2016).

334 The boundary conditions used for the permanent regime, Navier-Stokes, were:  
 335 i) Inlet: prescribed velocity; ii) Outlet: prescribed pressure; iii) Wall condition: non-slip.  
 336 The boundary conditions for the transient, passive scalar regime were: i) Inlet:  
 337 prescribed concentration of 100; ii) Outlet: null gradient; iii) Wall condition:  
 338 impermeable (null normal gradient).

339 The boundary conditions used for the permanent regime, Navier-Stokes, were: i)  
 340 Inlet: prescribed velocity; ii) Outlet: prescribed pressure; iii) Wall condition: non-slip.  
 341 The boundary conditions for the transient regime, passive scalar, were: i) Inlet:  
 342 prescribed concentration of 100; ii) Outlet: null gradient; iii) Wall condition:  
 343 impermeable (null normal gradient).

344 In Figure 1, the inlet, outlet and wall of the filter are indicated. The fluid velocity  
 345 at the entrance of the C-HSSFs was calculated by the ratio between the flow (48 L.day<sup>-1</sup>)  
 346 and the area of the entrance section.



347  
 348 Figure 1. Schematic of the C-HSSFs indicating the inlet, the outlet and the filter wall for  
 349 modelling purposes

350 In the I-HSSFs, the fluid velocity at the inlet was obtained from the average  
351 velocity calculated in the RTD experimental test. The average flow was obtained by the  
352 ratio between the volume of water and the total time of this test and then the velocity  
353 was calculated by the ratio between this flow and the area of the inlet section.

354 A time step was selected that guaranteed a Courant Number ( $Co$ ) or CFL  
355 criterion (Courant, Friedrichs and Lewy, 1967), less than 1, according to Eq. 8.

356 (8)

$$Co = \frac{U \cdot \Delta t}{\Delta}$$

357 Where parameter  $U$  is the local velocity [ $m \cdot s^{-1}$ ],  $\Delta t$  is the time step [s] and  $\Delta$  is  
358 the local length scale characteristic of the finite volumes of the mesh [m].

359 The Courant Number is a local parameter of the fluid, dimensionless domain,  
360 which represents the ratio between the characteristic physical time for the information to  
361 propagate the  $U$  velocity from one node in the mesh to the next, and the discrete time  
362 step used in the simulation. The use of longer time steps ( $Co > 1$ ) locally implies a  
363 violation of the transport physics of the property under analysis, which almost always  
364 results in numerical oscillations and/or divergence of the numerical solution.

365 After constructing the meshes with different refinements (variation in the number of  
366 finite elements), a mesh independence test was carried out. In this test, the velocity  
367 obtained for each mesh was analysed to determine from which degree of refinement the  
368 calculated values for velocity became independent of the mesh. Therefore, the minimum  
369 volume of the finite element ( $\Delta V$  [ $m^3$ ]) was obtained from the meshes generated in the  
370 CFD, adopting the Courant Number ( $Co$ ) of 0.9, according to Eq. 8 and Eq. 9.

371 (9)

$$\Delta = \sqrt[3]{\min(\Delta V)}$$

372 The condition used to verify the independence of the mesh was that the velocity  
 373 in the filter outlet, located at the centroid of the end of the outlet tube, did not present  
 374 variations greater than 5% of the real velocity.

375

### 376 2.2.1 Numerical method

377 Two geometries were created corresponding to each filter diameter (190 mm and  
 378 250 mm) and it is not necessary to construct four geometries (one per filter), since the  
 379 flow characteristic (continuous or intermittent) depends only on the boundary  
 380 conditions inserted in the simulation. The elaborated geometries followed the structure  
 381 shown in Figure 1.

382 Table 1 shows the numerical parameters used to simulate the filters and the RTD  
 383 simulations. The reference pressure adopted was 1 atm and the relative static pressure  
 384 was 0 atm, considering that the experiment was carried out close to sea level and the  
 385 flow was free. In the simulations carried out in a transient regime, that is, in the RTD  
 386 simulations, the following solution methods were used: i) Transient formulation of “first  
 387 implicit order”, ii) SIMPLE coupling scheme.

388

389 Table 1 – Numerical parameters for filter simulation and RTDs simulation

| Parameters                                | C-HSSF1                | C-HSSF2                | I-HSSF1                | I-HSSF2                |
|-------------------------------------------|------------------------|------------------------|------------------------|------------------------|
| Reference pressure [atm.]                 | 1                      | 1                      | 1                      | 1                      |
| Relative static pressure [atm.]           | 0                      | 0                      | 0                      | 0                      |
| Entrance section area [m <sup>2</sup> ]   | 0.0283                 | 0.0491                 | 0.0283                 | 0.0491                 |
| Inlet fluid velocity [m.s <sup>-1</sup> ] | 1.96 x10 <sup>-5</sup> | 1.13 x10 <sup>-5</sup> | 4.10 x10 <sup>-5</sup> | 5.66 x10 <sup>-5</sup> |
| Relative outlet pressure [atm.]           | 0                      | 0                      | 0                      | 0                      |
| Passive scalar value                      | 100                    | 100                    | 100                    | 0                      |

|                              |      |      |       |       |
|------------------------------|------|------|-------|-------|
| Time step (s)                | 23   | 56   | 600   | 600   |
| Number of time steps         | 1566 | 1072 | 13 30 | 12 24 |
| Maximum number of iterations | 15   | 15   | 15    | 15    |
| Total computational time (h) | 5    | 8    | 4     | 4     |

---

Notes: C-HSSF1 - continuous filter with a diameter of 190 mm; C-HSSF2: continuous filter with a diameter of 250 mm; I-HSSF1: intermittent filter with a diameter of 190 mm; and I-HSSF2: intermittent filter with a diameter of 250 mm.

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390

391 In I-HSSF1, a volume of 30 L was used in a time of 430 min and in I-HSSF2, 60  
392 L was applied in 360 min, obtained in the experimental tracer tests. The relative  
393 pressure at the outlet of 0 atm was used, as the flow depended only on the variation of  
394 the water level that preceded the layer of fine sand, that is, the flow was free.

395 The calculated values of viscous resistance ( $1/\alpha$ ) and inertial resistance ( $C_2$ ) were  
396 obtained based on the mean particle diameter ( $(D_p)$ ) and the void index ( $\epsilon$ ) values  
397 obtained in a laboratory test are contained in the supplementary material.

398 In the simulations carried out in the HSSFs steady state, the following solution  
399 methods were used: i) Pressure-velocity coupling scheme: SIMPLE (Semi-Implicit  
400 Method for Pressure Linked Equations); ii) spatial discretization of gradient “cells based  
401 on least squares”; iii) “second order” pressure spatial discretization; and iv) spatial  
402 discretization of “second-order upwind” momentum. The computational time for each  
403 of the simulations was approximately 2 hours and 400 iterations were used. The results  
404 of the simulations residues were less than  $1 \times 10^{-5}$ .

405 The dead zones were quantified by occupied volumes between velocities greater  
406 than 0 and less than  $1.05 \times 10^{-5} \text{ m.s}^{-1}$  for C-HSSF1,  $6.90 \times 10^{-6} \text{ m.s}^{-1}$  for C-HSSF2,  
407  $2.32 \times 10^{-5} \text{ m.s}^{-1}$  for the I-HSSF1 and  $2.22 \times 10^{-5} \text{ m.s}^{-1}$  for the I-HSSF2. These velocities

408 were determined punctually in the velocity contour plane where there was no formation  
409 of current lines. After defining this criterion and delineating the dead zone, its volume  
410 can be calculated in relation to the sum of the volumes of the filtering and draining  
411 layers. The images of the current lines and the velocity contour plane are shown in the  
412 supplementary material.

### 413 **2.2.2 RTD simulation**

414 The determination of the residence time distribution with CFD used the passive  
415 scalar equation (TALVY et al., 2011) for a transient regime as a solution for using a  
416 tracer concentration in the model.

417 The transport of a passive scalar refers to the convection-diffusion of a scalar  
418 field within the fluid in motion without significant changes in the properties of the fluid  
419 under analysis, such as in the velocity field, pressure and temperature, hence the term  
420 passive. Eq. 10 was used to calculate the passive scalar, and thus solve the tracer test in  
421 the model (ANSYS, 2013).

422 (10)

$$\frac{\partial \rho C}{\partial t} + \nabla \cdot (\rho UC) = \nabla \cdot (D_{disp} \nabla C)$$

423 Where:  $\rho$  is the density of the fluid in  $\text{kg.m}^{-3}$ ;  $C$  is the tracer concentration in  
424  $\text{mg.L}^{-1}$ ;  $U$  is the velocity vector in  $\text{m.s}^{-1}$ ; and  $D_{disp}$  is the dispersion coefficient given in  
425  $\text{m}^2.\text{s}^{-1}$ .

426 In this equation, the first term on the left side of the equality corresponds to the  
427 concentration of solute in the solvent over time, the second term corresponds to the  
428 advective term of concentration carried by the velocity field; and the one on the right  
429 side of equality, the term corresponds to the diffusive term of concentration.

430 The ANSYS Fluent software solves the transport equation for a passive scalar  
431 defined by the user as User-defined scalar (UDS) in the same way as it solves the

432 transport equation for a scalar such as mass fraction (ANSYS, 2013). For transient  
433 simulations, the governing equations were discretized in space and time.

434 In the CFD tracer test, the diffusion coefficient at 25 ° C of NaCl corresponding  
435 to  $1.612 \times 10^{-9} \text{ m}^2 \cdot \text{s}^{-1}$  with diffusivity of  $1.609 \times 10^{-6} \text{ kg} \cdot \text{m}^{-1} \cdot \text{s}^{-1}$  was used, as established by  
436 Robinson and Stoke (1955). In the tests of C-HSSFs and I-HSSFs, the dimensionless  
437 scalar value of 100 was used to refer to the  $100 \text{ mg} \cdot \text{L}^{-1}$  salt solution and 0 for the other  
438 tap water feeds. The outgoing concentration of the passive scalar was obtained by the  
439 integral of the outgoing section area.

440

### 441 **2.3. Model validation and verification**

442 Furman & Stegowski (2011) suggested the following steps to verify the CFD  
443 results: i) Choose the CFD model appropriately from the physical point of view of the  
444 problem; ii) obtain the velocity field and the RTD simulation with CFD; iii) evaluate the  
445 deviation of the results of the experimental RTD and RTD predicted with CFD; and iv)  
446 analyse the velocity fields if they are different simulated geometries.

447 The article presents the flow simulations applied in HSSFs using the Ansys  
448 Fluent 2020 R2 to analyse the influence of continuous (C-HSSF) and intermittent (I-  
449 HSSF) feeds and geometric shape changes on the hydrodynamic behaviour of the filter.

450

### 451 **2.4. Statistical analysis**

452 A priori the data sets were assessed for normality by the Shapiro-Wilk test,  
453 which allowed us to classify each data set as: data with normal distribution (Shapiro-  
454 Wilk test  $p > 0.05$ ) in which parametric tests are applied or data with non-normal  
455 distribution (Shapiro-Wilk test  $p < 0.05$ ) in which non-parametric tests are applied.

456 The statistical analysis used to validate experimental and computational RTD  
457 tests was performed using the Kruskal-Wallis non-parametric test (95% confidence  
458 limit) followed by the Mann-Whitney pairwise test, indicated when comparing three or  
459 more groups, to perform the tests, the free access software PAST 4.03  
460 (PAlaeontological STatistics) was used.

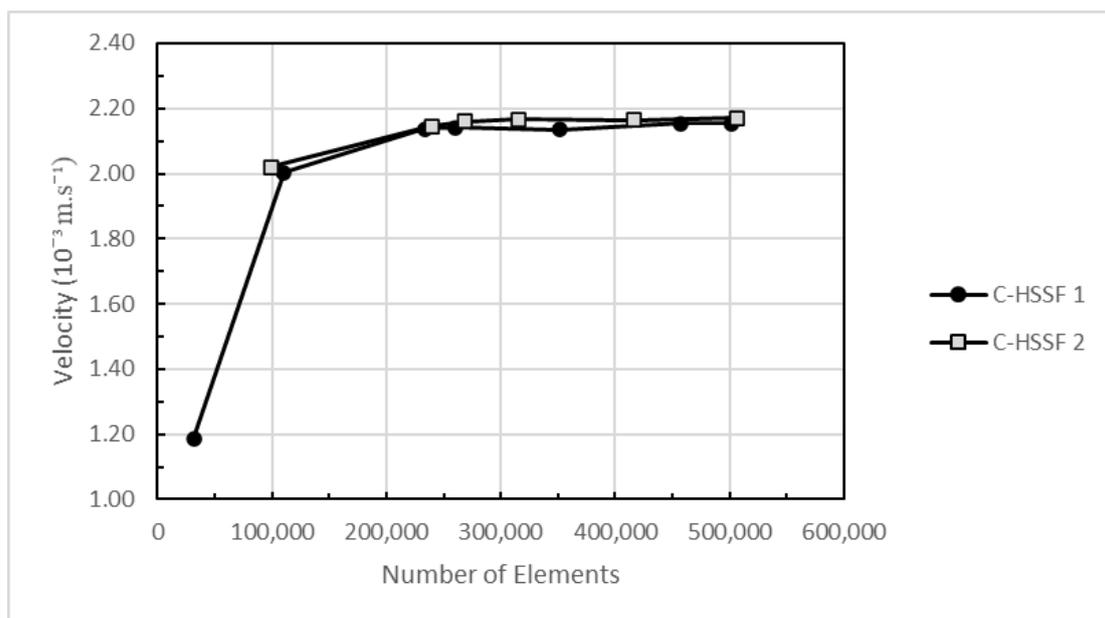
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### 462 3. Results and discussion

#### 463 3.1. Numerical Results

464 In steady state simulations, the outlet velocities were obtained, located in the  
465 centre of the outlet tube, that is, in the centroid of the end of the outlet tube. The  
466 behaviour of this velocity was analysed as a function of the control volumes, as shown  
467 in Figure 2. It can be seen that the minimum value required for variations not greater  
468 than 5% for the C-HSSF1 was 233,264 elements (Figure 3A) and for C-HSSF2 it was  
469 268,474 elements (Figure 3B).

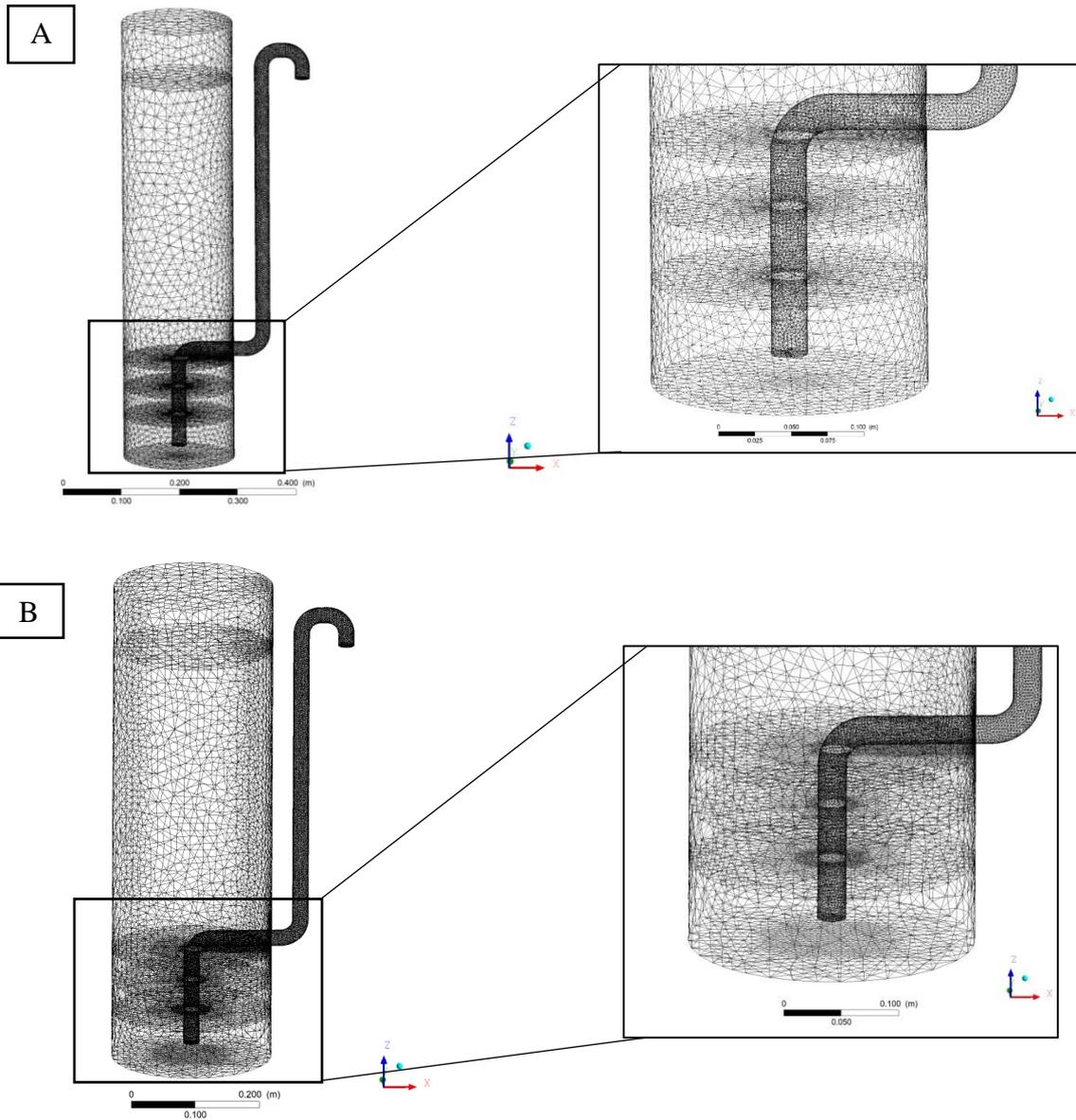
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471

472 Figure 2 – Velocity as a function of the number of elements of the numerical grid  
473 obtained in the mesh independence test of C-HSSF1 and C-HSSF2 using Ansys®  
474 Software 19.2.

475



476 Figure 3 – Meshes obtained for C-HSSF1 and C-HSSF2.

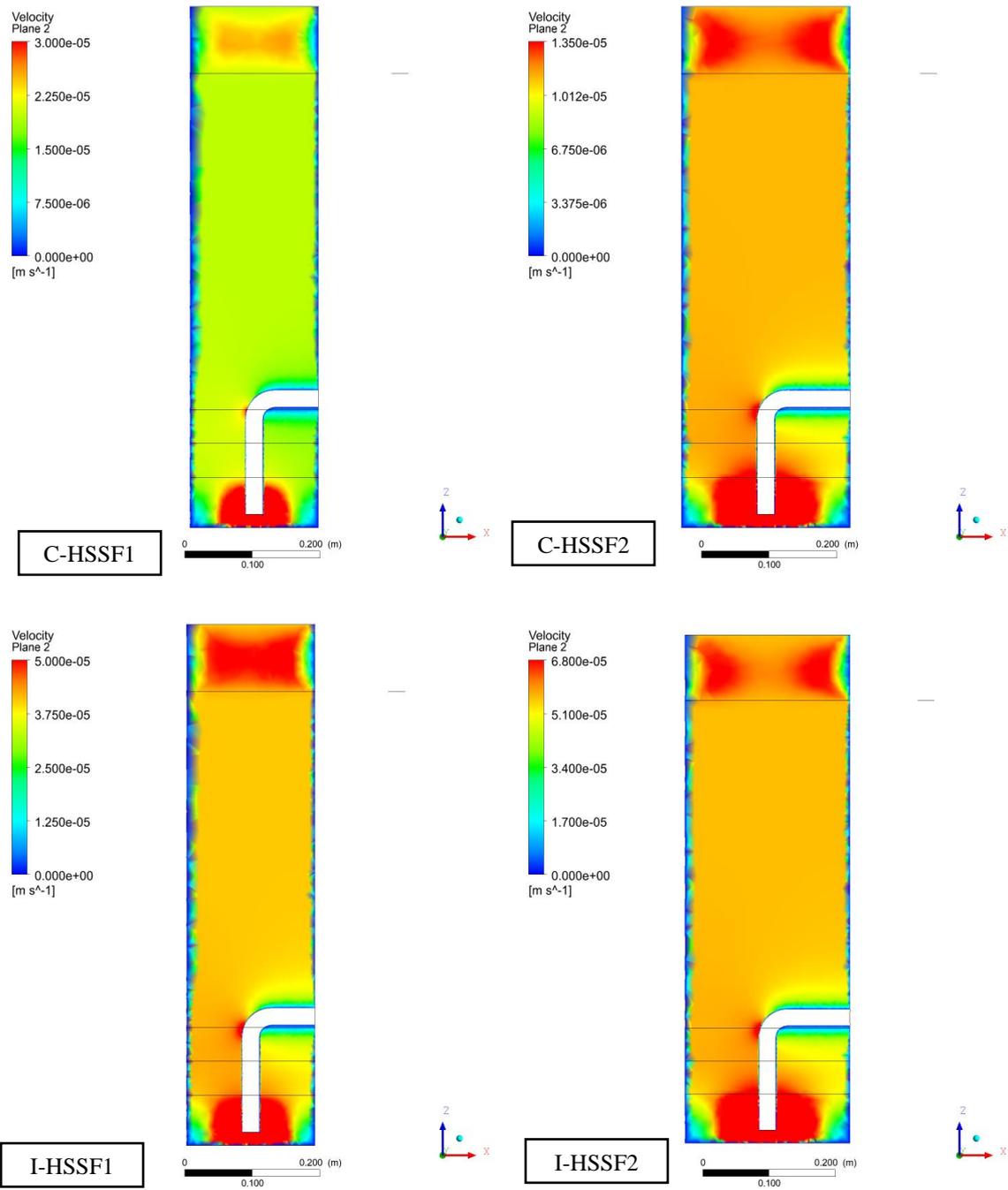
477 Legend: Figure 3A (C-HSSF1 with 233,264 elements of tetrahedral type); and Figure  
478 3B (C-HSSF2 with 268,474 elements of tetrahedral type).

479

480 According to the results, the current lines showed symmetry in relation to the  
481 central axis, the existence of a dead zone near the base of the HSSF in the coarse gravel  
482 layer and the absence of a short circuit. Similar behaviour was described by Berbert et  
483 al. (2016) who found the symmetry and dead zone in HSSF, without obtaining the  
484 volume of the dead zone, with the same output configuration used in the present study.

485 In the simulated HSSFs, the locations of the dead zone were defined, and the  
486 volumes were obtained. The percentage results of the volume of the dead zones in  
487 relation to the sum of the volumes of the filtering and draining layers were: C-HSSF1  
488 2.19%, C-HSSF2 2.99%, I-HSSF1 2.37% and I-HSSF2 2.60%. It was found that the  
489 values were low, below 3%, and the behaviour of the current lines in the HSSFs were  
490 similar, regardless of the geometry or type of flow. It was also found that for the same  
491 type of flow regime, whether in continuous or intermittent flow, the increase in diameter  
492 implied an increase in the volume of the dead zone. The results of the dead zone  
493 volumes are shown in the supplementary material.

494 The velocity profiles in the XZ plane at the centre of the HSSFs were visually  
495 similar, as seen in Figure 4. The velocity scale was previously defined, and the outlet  
496 tube was removed from the visualization for a better analysis of the velocity variation  
497 inside the filters. It was found that in the water layer the velocity was higher than when  
498 it reached the filtering and draining layers, and then increased in the coarse gravel layer  
499 before reaching the water outlet.



500 Figure 4 – Velocity profiles on the XZ plane located in the center of the HSSFs

501 indicating the maximum and minimum velocities

502

503 In the simulations, the velocities were sampled in the centroid of the filter,

504 located in the layer of fine sand, and the velocities of the real experiments were

505 compatible (Table 2), which indicates the representativeness of the mathematical  
 506 models in relation to the HSSFs built in real scale.

507

508 Table 2 - Velocity of experimental and simulated HSSFs

| HSSF    | Velocity (m.s <sup>-1</sup> ) |                        | Difference (%) |
|---------|-------------------------------|------------------------|----------------|
|         | Experimental                  | Simulation             |                |
| C-HSSF1 | 1.959x10 <sup>-5</sup>        | 1.956x10 <sup>-5</sup> | -0.15          |
| C-HSSF2 | 1.132x10 <sup>-5</sup>        | 1.129x10 <sup>-5</sup> | -0.27          |
| I-HSSF1 | 4.10x10 <sup>-5</sup>         | 4.092x10 <sup>-5</sup> | -2.44          |
| I-HSSF2 | 5.66x10 <sup>-5</sup>         | 5.648x10 <sup>-5</sup> | -2.83          |

509

510 The velocity profiles obtained for the HSSFs, as shown in Figure 5, show that at  
 511 the initial points on the water slide the velocity is higher and then there is a reduction  
 512 when it starts to percolate through the filter layer. The velocity remains constant until  
 513 reaching the last layers, when there is an increase close to the water outlet/treated water  
 514 collection region and the last point shows the velocity close to the wall at the bottom of  
 515 the filter. The increase in velocity near the water outlet corroborates the observations of  
 516 Berbert et al. (2016).

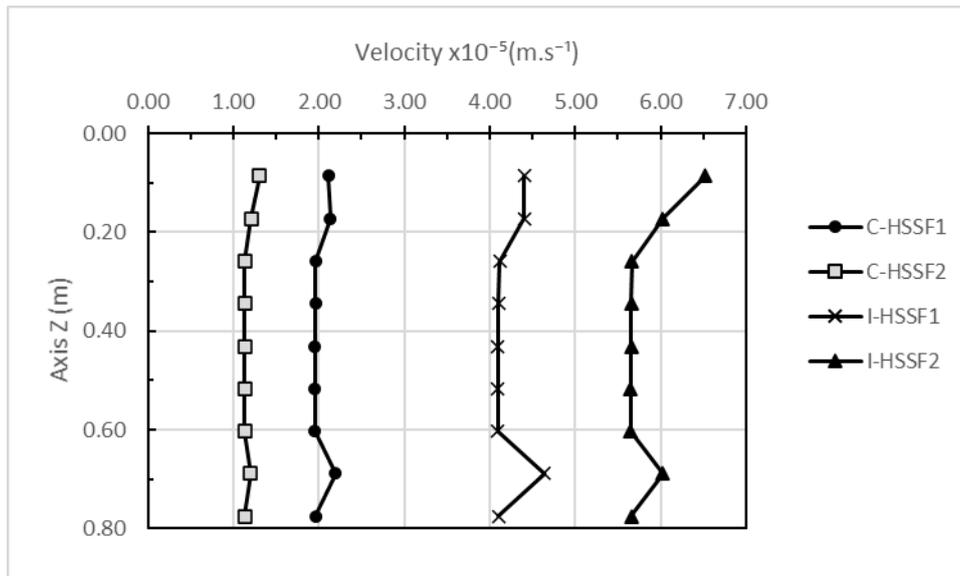


Figure 5 – Velocity profiles of HSSFs.

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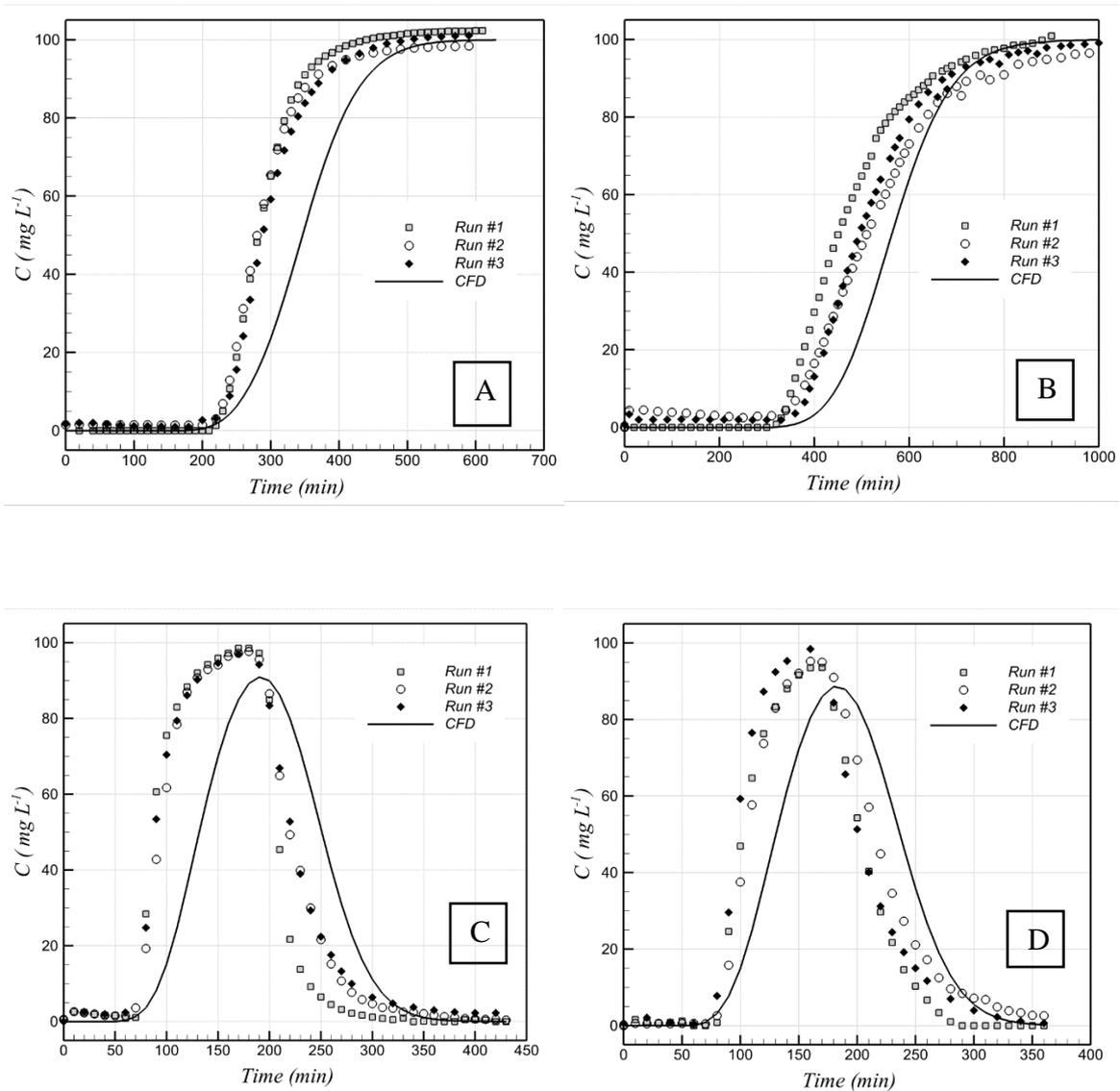
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531

### 532 3.2. Comparison between experimental and simulated RTD (CFD)

533

534 Table 2 shows that the velocities obtained in the simulation were close to and  
 535 below the experimental velocities and the analysis of the results obtained with the  
 536 experimental tracer tests and the CFD tracer test, presented in Figure 6, can classify the  
 537 HSSFs as a plug flow reactor.  
 538



539 Figure 6 – Experimental and computational RTD of HSSFs.

540 Notes: A - C-HSSF1; B - C-HSSF2; C - I-HSSF1; and D - I-HSSF2.

541

542 The results obtained in the I-HSSFs corroborate the behaviours described by  
543 Andreoli and Sabogal-Paz (2020), Bradley et al. (2011), Elliott et al. (2008), Maciel and  
544 Sabogal-Paz (2020) and Terin and Sabogal-Paz (2019), who characterized the HSSF as  
545 a plug flow reactor.

546 According to the adaptation of the MDI to the mMDI proposed by Lynn et al.  
547 (2013), they presented mMDI results of 2.92. In the I-HSSFs of Andreoli and Sabogal-  
548 Paz (2020), the MDI values were 2.19 and 2.21 and the mMDI results were 2.47 and  
549 2.56, respectively, and Sabogal-Paz et al. (2020) reported mMDI values of 0.95. In the  
550 study, the results of the mMDI for I-HSSF 1 were  $2.22 \pm 0.132$  and for I-HSSF 2, it was  
551  $2.04 \pm 0.082$ , which is close to the results obtained by Andreoli and Sabogal-Paz (2020).

552 The residence time distribution for C-HSSF 1 was  $293 \pm 6$  min and for C-HSSF 2,  
553 it was  $462 \pm 79$  min. These values are close to the theoretical residence time distribution  
554 of  $300 \pm 8$  min and  $450 \pm 13$  min for C-HSSF1 and C-HSSF2, respectively. The  
555 adjustment data for the N-CSTR model and for the models with small and large  
556 dispersion of the C-HSSFs are shown in Table 3. In the C-HSSF 1 (cross-sectional area  
557 =  $0.028 \text{ m}^2$ ), the N-CSTR model presented the best result, requiring 22 complete mix  
558 reactors in series. The largest number of reactors in series indicates a plug flow reactor  
559 (Levenspiel, 1999). The C-HSSFs studied by Sabogal-Paz et al. (2020) presented  $N =$   
560 17 (filter cross-section of  $0.0075 \text{ m}^2$ ). Those tested by Andreoli and Sabogal-Paz (2020)  
561 obtained  $N = 8$  and  $N = 13$  (filter cross-sectional area of  $0.049 \text{ m}^2$ ) and those tested by  
562 Terin and Sabogal-Paz (2019) had  $N = 6$  (filter cross-sectional area of  $0.049 \text{ m}^2$ ). In the  
563 C-HSSF 2, the piston model with great dispersion had the best result. Although C-  
564 HSSF1 and C-HSSF 2 fit different models, the results of both refer to a plug flow  
565 reactor.

566

567 Table 3 - Tracer test results for the C-HSSF

| HSSF    | Statistic          | N-CSTR |                | Small dispersion model |                | High dispersion model |                |
|---------|--------------------|--------|----------------|------------------------|----------------|-----------------------|----------------|
|         |                    | N      | r <sup>2</sup> | D, μL <sup>-1</sup>    | r <sup>2</sup> | D, μL <sup>-1</sup>   | r <sup>2</sup> |
| C-HSSF1 | Mean               | 22     | 0.86           | 0.02                   | 0.82           | 0.02                  | 0.80           |
|         | Standard deviation | 6      | 0.05           | 0.01                   | 0.04           | 0.01                  | 0.03           |
| C-HSSF2 | Mean               | 10     | 0.64           | 0.05                   | 0.63           | 0.05                  | 0.68           |
|         | Standard deviation | 2      | 0.14           | 0.01                   | 0.10           | 0.01                  | 0.07           |

568

569 The flow in piston flow observed in I-HSSFs and C-HSSFs is good because it  
 570 shows that the treatment will be homogeneous in all water fractions that enter the filter.  
 571 Sabogal-Paz et al. (2020) suggested that the piston flow reactor improved the  
 572 development of the biological layer and the efficiency of the treatment.

573 Figure 6 shows the comparison between experimental and simulated RTD for C-  
 574 HSSFs and I-HSSFs. Results from CFD simulations are validated with experimental  
 575 RTD tests (Brannock et al., 2010; Furman & Stegowski, 2011; Gharibian et al., 2020;  
 576 Klusener et al., 2007; Qi et al., 2013; Talvy et al., 2011; Zhang et al., 2007). The  
 577 computational RTDs of the I-HSSF1 and I-HSSF2 show that the simulations present a  
 578 perfect Gaussian distribution, as expected for the simulation.

579 The form of data collection may have influenced the signal obtained  
 580 experimentally, which shows the difference observed in the results of the experimental  
 581 and simulated RTDs, as was found by Talvy et al. (2011) who chose to modify the  
 582 simulated RTD to fit the experimental RTD. It is noteworthy that the RTDs were

583 simulated using the average velocity and constant values of the boundary condition,  
584 such as porosity and permeability. When the real experiment was constructed, the layers  
585 may have undergone natural and anthropic compaction, accommodating the grains  
586 during assembly and feeding, and presented values different from those obtained in the  
587 laboratory, which may explain the delay in the response time to the stimulus of the  
588 simulated HSSFs compared to the experimental ones.

589         The Kruskal Wallis non-parametric test (5% significance level) showed that the  
590 results of the three experimental tests of the RTDs and the computational test of the  
591 RTD did not show statistically significant differences between each other for each of the  
592 filters. The C-FLD 1, C-FLD 2, I-FLD 1 and I-FLD2 had a p-value of 0.27; 0.25; 0.01  
593 and 0.38. Thus, the RTD result obtained with CFD is like the results of RTDs obtained  
594 experimentally in full-scale physical models, as there was no significant difference  
595 between the results.

596         The numerical simulations of the RTDs were validated with the experimental  
597 tests of the RTDs, and therefore the hydrodynamics of the HSSFs were analysed. The  
598 behaviour of the current lines of the C-FLDs and I-FLDs were similar and showed that  
599 they are not influenced due to the geometry, the filtration rate, or the type of continuous  
600 or intermittent feeding. In the C-FLDs and I-FLDs, it was found that the flow was of the  
601 piston type, with no short circuit and having a dead zone close to the base. The smaller  
602 the diameter, the smaller the dead zone. The C-HSSFs showed minimization adverse  
603 hydraulic phenomena, as seen by the lower variation of the filter velocity profile, which  
604 may reflect in the improvement of treatment efficiency due to the reduction of  
605 interferences in the development of the biological layer.

606

#### 607 **4. Conclusions**

608           The behaviour of the C-HSSFs and I-HSSFs flow lines were similar according to  
609 the visual analysis of the 3D flow lines (supplementary material). In the C-HSSFs and I-  
610 HSSFs, it was found that the flow was of the piston type, with no short circuit and  
611 having a dead zone close to the base. The piston flow is good for the treatment because  
612 the incoming water will be treated at the same time in all its portions, favouring the  
613 efficiency of the HSSF.

614           The flow of the piston type is desirable for HSSFs, as it allows biological  
615 treatment to occur at the beginning of the filter layer and, concomitantly, physical-  
616 chemical treatments occur as the water percolates through the filter layer until the  
617 treated water is obtained at the end of layers, that is, the incoming water will be treated  
618 at the same time in all its portions as it percolates through the filter media.

619           The volumes of the dead zone in the HSSFs were less than 3%, and due to this  
620 low value, there was no need to change the design of the HSSFs. The statistical results  
621 showed that there were no significant differences in the statistical comparison of the  
622 data from the experimental and simulated RTDs.

623           In view of this and considering that all filters showed flow of the piston type, the  
624 choice of geometry and type of feed depends on studies of the analysis of treatment  
625 efficiency considering the water quality parameters.

626

## 627 **Acknowledgements**

628

629 This work was supported by the Global Challenges Research Fund (GCRF) UK  
630 Research and Innovation (SAFEWATER; EPSRC Grant Reference EP/P032427/1).

631

## 632 **Statement**

633

634           The authors hereby declare previous originality check, no conflict of interest and  
635 open access to the repository of data used in this paper for scientific purposes.

636

### 637 **Supplementary Material**

638

639           Brazilian standards used in the physical characterization of materials and  
640 experimental results are provided as supplementary material.

641

### 642 **References**

643 Andreoli, F. C., Sabogal-Paz, L. P., 2020. Household slow sand filter to treat  
644 groundwater with microbiological risks in rural communities. *Water Research*. 186,  
645 116352. <https://doi.org/10.1016/j.watres.2020.116352>.

646 ANSYS, Inc., *Ansys fluent User's Guide*, 2013. Release 15.0, ANSYS, Canonsburg,  
647 United States of América.

648 Berbert, A. C., Almeida, R. A de, Rezende, R. V. de P., Lautenschlager, S. R. The use  
649 of computation fluids dynamics to select outlet system configuration in biosand  
650 filters. Conference: 13th IWA Specialized Conference on Small Water and  
651 Wastewater Systems & 5th IWA Specialized Conference on Resources-Oriented  
652 Sanitation At: Athens, September, 2016.

653 Botari, A., Di Bernardo, L., 2012. Hydrodynamic analysis of particle collection  
654 efficiency: comparing downflow and upflow filtration. *Acta Scientiarum*.  
655 *Technology*, v. 34, n. 2, p. 167-175. doi:10.4025/actascitechnol.v34i2.10803.

656 Brannock, M., Wang, Y., Leslie, G., 2010. Mixing characterisation of full-scale  
657 membrane bioreactors: CFD modelling with experimental validation. *Water*  
658 *Research* 44 (10), 3181–3191. <https://doi.org/10.1016/j.watres.2010.02.029>.

659 Bradley, I., Straub, A., Maraccini, P., Markazi, S., Nguyen, T.H., 2011. Iron oxide  
660 amended biosand filters for virus removal. *Water Res* 45, 4501–4510.  
661 doi:10.1016/j.watres.2011.05.045.

662 Campos, L.C., Smith, S.R., Graham, N.J.D, 2006a. Deterministic based model of slow  
663 sand filtration. I: model development. *Journal of Environmental Engineering* 132(8),  
664 872-886. [https://doi.org/10.1061/\(ASCE\)0733-9372\(2006\)132:8\(872\)](https://doi.org/10.1061/(ASCE)0733-9372(2006)132:8(872)).

665 Campos, L.C., Smith, S.R., Graham, N.J.D, 2006b. Deterministic based model of slow  
666 sand filtration. II: model application. *Journal of Environmental Engineering* 132(8),  
667 887-894. [https://doi.org/10.1061/\(ASCE\)0733-9372\(2006\)132:8\(887\)](https://doi.org/10.1061/(ASCE)0733-9372(2006)132:8(887)).

668 CAWST, 2012. Biosand Filter Construction Manual. Centre for affordable water and  
669 sanitation. Canada, Calgary.

670 CAWST, 2009. Biosand filter manual: Design, construction, installation, operation and  
671 maintenance, Canada, Calgary, Canada.

672 Courant, R., K. Friedrichs e H. Lewy. On the Partial Difference Equations of  
673 Mathematics Physics. *IBM Journal*, n. March, p. 215-234. 1967.

674 Dadonaite, B., Ritchie, H., Roser, M., 2020. Diarrheal diseases. Published online at  
675 OurWorldInData.org. (<https://ourworldindata.org/diarrheal-diseases>, accessed 19  
676 May 2020).

677 Darcy, H. Les fontaines publiques de la ville de Dijon. Paris: Victor Dalmont, 1856. 647  
678 p.

679 Elliott, M.A., Stauber, C.E., Koksal, F., DiGiano, F.A., Sobsey, M.D., 2008. Reductions  
680 of *E. coli*, echovirus type 12 and bacteriophages in an intermittently operated

681 household-scale slow sand filter. *Water Res* 42, 2662–2670.  
682 doi:10.1016/j.watres.2008.01.016.

683 Ergun, S. Fluid flow through packed columns. *Chemical Engineering Progress*, v. 48, n.  
684 2, p. 89-94, 1952.

685 Forchheimer, P. Wasserbewegung durch Boden. *Zeitschrift des Vereins Deutscher*  
686 *Ingenieure*, v. 45, n. 49, p. 1736-1741, 1901a.

687 Forchheimer, P. Wasserbewegung durch Boden. *Zeitschrift des Vereins Deutscher*  
688 *Ingenieure*, v. 45, n. 50, p. 1781-1788, 1901b.

689 Furman, L., Stegowski, Z., 2011. CFD models of jet mixing and their validation by  
690 tracer experiments. *Chemical Engineering and Processing: Process Intensification*  
691 50(3), 300–304. <https://doi.org/10.1016/j.cep.2011.01.007>.

692 Gharibian, S., Hazrati, H., Rostamizadeh, M. 2020. Continuous electrooxidation of  
693 Methylene Blue in filter press electrochemical flowcell: CFD simulation and RTD  
694 validation. *Chemical Engineering & Processing: Process Intensification*. 150 (2020)  
695 107880. <https://doi.org/10.1016/j.cep.2020.107880>.

696 Jadhav, D., Husain, M., Chavan, F.I., 2015. Biosand Water Filter: A Boon. *International*  
697 *Research Journal of Engineering and Technology* 2 (3).  
698 <https://www.irjet.net/archives/V2/i3/Irjet-v2i3262.pdf>

699 Kennedy, T. J., Hernandez, E. A., Morse, A. N., Anderson, T. A. 2012. Hydraulic  
700 Loading Rate Effect on Removal Rates in a BioSand Filter: A Pilot Study of Three  
701 Conditions. *Water, Air, & Soil Pollution*, 223 (7), 4527-4537.  
702 <https://link.springer.com/article/10.1007/s11270-012-1215-4>.

703 Kikkawa, I. 2008. Modification of a Biosand Filter in the Northern Region of Ghana.  
704 Master of Engineering in Civil and Environmental Engineering at the Massachusetts  
705 Institute of Technology.

706 Klusener, P. A. A., Jonkers, G., During, F., Hollander, E. D., Schellekens, C. J.,  
707 Ploemen, I. H. J., Othman, A., Bos, A. N. R., 2007. Horizontal cross-flow bubble  
708 column reactors: CFD and validation by plant scale tracer experiments. Chemical  
709 Engineering Science 62(18–20), 5495–5502.  
710 <https://doi.org/10.1016/j.ces.2007.03.044>.

711 Langergraber, G., Giraldi, D., Mena, J., Meyer, D., Peña, M., Toscano, A., Brovelli, A.,  
712 Korkusuz, E. A., 2009. Recent developments in numerical modelling of subsur-face  
713 flow constructed wetlands. Science of The Total Environment 407 (13), 3931–3943.  
714 <https://doi.org/10.1016/j.scitotenv.2008.07.057>.

715 Levenspiel, O., 1999. Chemical Reaction Engineering, Industrial & Engineering  
716 Chemistry Research. <https://doi.org/10.1021/ie990488g>.

717 Lynn, T.J., Wanjugi, P., Harwood, V.J., Ergas, S.J., 2013. Dynamic performance of  
718 biosand filters. J. Am. Water Works Assoc. 105 (10), E587–E595.  
719 <https://doi.org/10.5942/jawwa.2013.105.0116>.

720 Maciel, P. M. F.; Sabogal-Paz, L. P. (2020). Household slow sand filters with and  
721 without water level control: continuous and intermittent flow efficiencies.  
722 Environmental Technology, 41(8), 944-958.  
723 <https://doi.org/10.1080/09593330.2018.1515988>.

724 Navier, C. L. M. H. Mémoire sur les lois du mouvement des fluides. Mémoires de l'  
725 Académie Royale des Sciences de l'Institut de France, v.6, p. 389-440, 1823.

726 Qi, W. K.; Guo, Y. L.; Xue, M.; LI, Y. Y. 2013. Hydraulic analysis of an upflow sand  
727 filter: Tracer experiments, mathematical model and CFD computation. Chemical  
728 Engineering Science. 104, 460-472. <https://doi.org/10.1016/j.ces.2013.09.035>.

729 Robinson, R. A.; Stoke, R. H. 1955. Electrolyte solutions. Butterworths Publications.  
730 Londres.

731 Sabogal-Paz, L. P.; Campos, L. C.; Bogush, A.; Canales, M. 2020. Household slow  
732 sand filters in intermittent and continuous flows to treat water containing low mineral  
733 ion concentrations and Bisphenol A. *Science of the Total Environment*. 702, 135078.  
734 <https://doi.org/10.1016/j.scitotenv.2019.135078>.

735 Sobsey, M.D., Stauber, C.E., Casanova, L.M., Brown, J.M., Elliot, M.A., 2008. Point of  
736 use household drinking water filtration: a practical, effective solution for providing  
737 sustained access to safe drinking water in the developing World. *Environ. Sci.*  
738 *Technol.* 42, 4261e4267. <https://doi.org/10.1021/es702746n>.

739 Stokes, G. G. On the theories of internal friction of fluids in motion and of the  
740 equilibrium and motion of elastic solids. *Transactions of the Cambridge*  
741 *Philosophical Society*, v. 8, p. 207-305, 1845.

742 Stropky, D.; Pougatch, K.; Nowak, P.; Salcudean, M.; Pagoria, P.; Gartshore, I.; Yuan,  
743 J. 2007. RTD (residence time distribution) predictions in large mechanically aerated  
744 lagoons. *Water Science & Technology*. 55, 11, 29-36.  
745 <https://doi.org/10.2166/wst.2007.346>.

746 Talvy, S.; Debaste, F.; Martinelli, L.; Chauveheid, E.; HAUT, B. 2011. Development of  
747 a tool, using CFD, for the assessment of the disinfection process by ozonation in  
748 industrial scale drinking water treatment plants. *Chemical Engineering Science*. 66,  
749 3185-3194. <https://doi.org/10.1016/j.ces.2011.02.039>.

750 Tchobanoglous, G., Burton, F.L., Stensel, H.D., 2003. *Wastewater Engineering:*  
751 *Treatment and Reuse*. McGraw-Hill Higher Education, New York.

752 Terin, U. C.; Sabogal-Paz, L. P. 2019. *Microcystis aeruginosa* and microcystin-LR  
753 removal by household slow sand filters operating in continuous and intermittent  
754 flows. *Water Research*. 150, 29-39. <https://doi.org/10.1016/j.watres.2018.11.055>.

755 United Nations Environment Programme (UNEP). 2016. A Snapshot of the World's  
756 Water Quality: Towards a global assessment. Unites Nations Environment  
757 Programme, Nairóbi, Quénia.

758 YOUNG-ROJANSCHI, C.; MADRAMOOTOO, C. Comparing the performance of  
759 biosand filters operated with multiday residence periods. Journal of Water Supply:  
760 Research and Technology-Aqua. 64, 157. 2014a.  
761 <https://doi.org/10.2166/aqua.2014.027>.

762 YOUNG-ROJANSCHI, C; MADRAMOOTOO, C. Intermittent Versus Continuous  
763 Operation of Biosand Filters. Water Research v. 45. 1-10 p., 2014b

764 Zhang, L., Pan, Q., Rempel, G.L., 2007. Residence time distribution in a multistage  
765 agitated contactor with Newtonian fluids: CFD prediction and experimental  
766 validation. Industrial and Engineering Chemistry Research 46 (11), 3538-3546.  
767 <https://doi.org/10.1021/ie060567+>.

768

**Supplementary Material**

769

770

771 Table S1 – Standards used in the physical characterization of materials

| Materials     | Granulometry           | CU <sup>1</sup>  | Specific mass    | Voids index   | Permeability           |
|---------------|------------------------|------------------|------------------|---------------|------------------------|
| Fine sand     | ABNT NBR<br>11799/2016 |                  |                  |               |                        |
| Coarse sand   |                        | ABNT             | ABNT             | ABNT          | ABNT NBR<br>13292/1995 |
| Fine gravel   | ABNT NM<br>248/2001    | NBR<br>6502/1995 | NBR<br>6458/2016 | NM<br>45/2006 |                        |
| Coarse gravel |                        |                  |                  |               |                        |

772 Notes: <sup>1</sup> Coefficient of uniformity (CU).

773

774 Table S2 – Specific mass, voids index and material of permeability

| Materials     | Specific mass<br>(g.cm <sup>-3</sup> ) | Voids index | Permeability<br>(cm.s <sup>-1</sup> ) |
|---------------|----------------------------------------|-------------|---------------------------------------|
| Fine sand     | 2.66                                   | 0.40        | 1.97 x 10 <sup>-2</sup>               |
| Coarse sand   | 2.64                                   | 0.46        | 1.06 10 <sup>-1</sup>                 |
| Fine gravel   | 2.63                                   | 0.43        | 4.75                                  |
| Coarse gravel | 2.64                                   | 0.39        | 8.28                                  |

775

776 Table S3 - Characteristics of the porous media of the filters

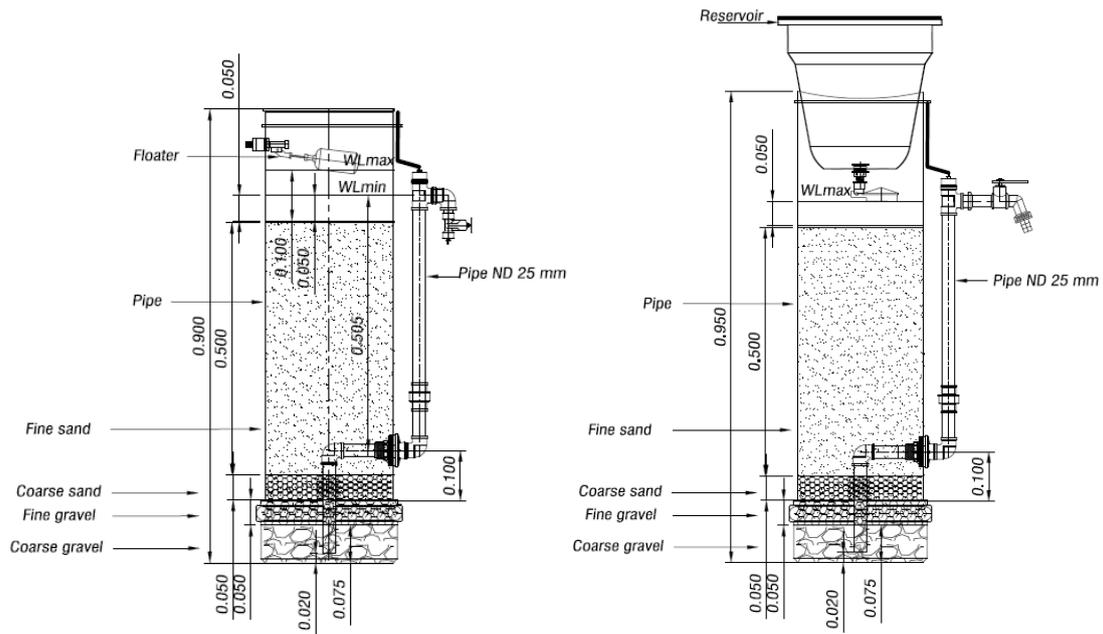
| Filter materials | D <sub>p</sub> (m)     | ε ( ) | α (m <sup>2</sup> )     | 1/α (m <sup>-2</sup> ) | C <sub>2</sub> (m <sup>-1</sup> ) |
|------------------|------------------------|-------|-------------------------|------------------------|-----------------------------------|
| Fine sand        | 2.70 x10 <sup>-4</sup> | 0.40  | 8.64 x10 <sup>-11</sup> | 1.16 x10 <sup>10</sup> | 1.21 x10 <sup>5</sup>             |
| Coarse sand      | 1.30 x10 <sup>-3</sup> | 0.46  | 3.76 x10 <sup>-9</sup>  | 2.66 x10 <sup>8</sup>  | 1.49 x10 <sup>4</sup>             |
| Fine gravel      | 4.00 x10 <sup>-3</sup> | 0.43  | 2.61 x10 <sup>-8</sup>  | 3.83 x10 <sup>7</sup>  | 6.27 x10 <sup>3</sup>             |
| Coarse gravel    | 1.04 x10 <sup>-2</sup> | 0.39  | 1.15 x10 <sup>-7</sup>  | 8.70 x10 <sup>6</sup>  | 3.46 x10 <sup>3</sup>             |

777 Notes: 1/α: viscous resistance, C<sub>2</sub>: inertial resistance, D<sub>p</sub>: average particle diameter, ε:

778 voids index

779

780



781

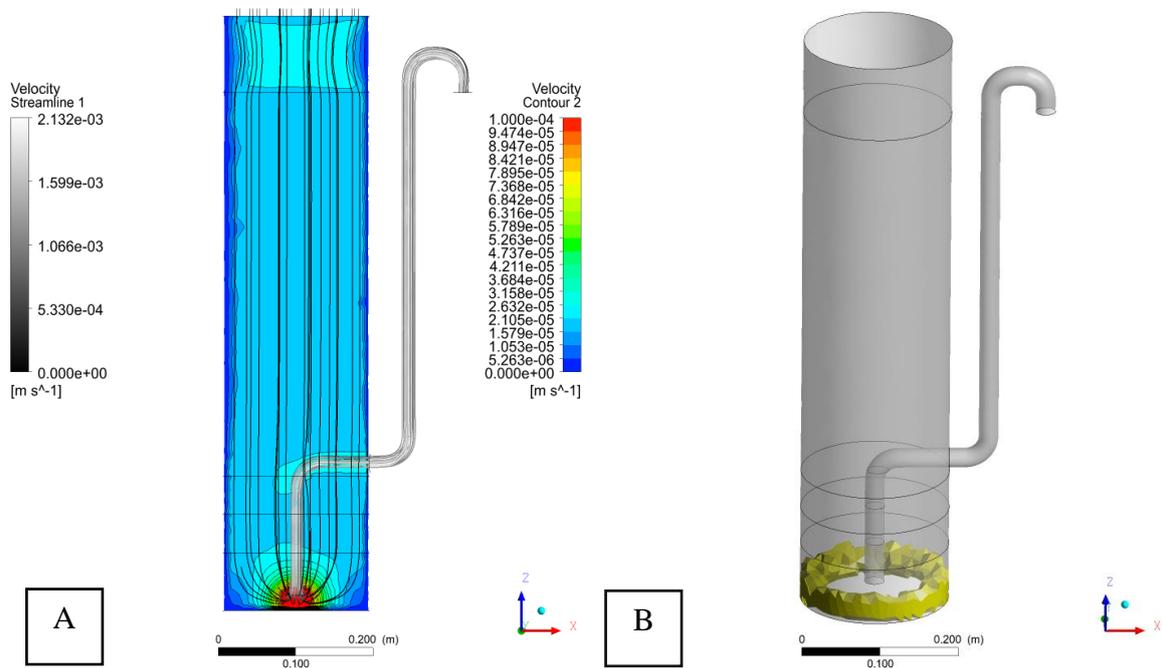
782 Continuous flow (C-HSSF)

Intermittent flow (I-HSSF)

783

Figure S1. Scheme of the studied HSSFs (units in meters)

784

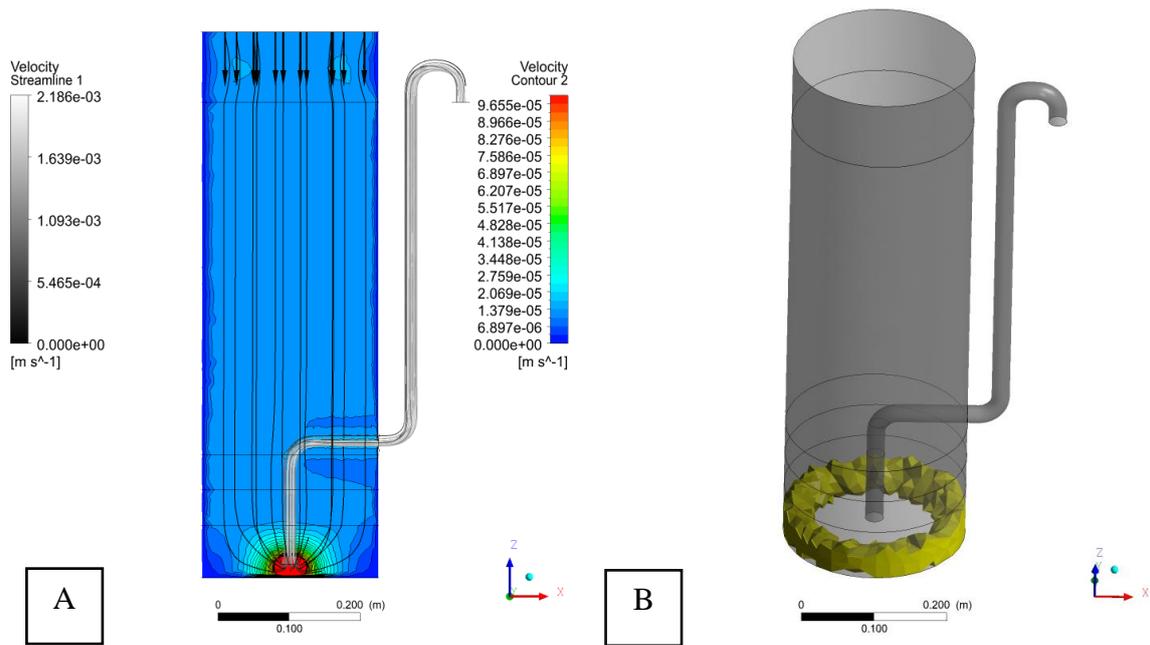


785 Figure S2 – Dead zone in C-HSSF1 (A - Current lines and velocity contour plane; B -

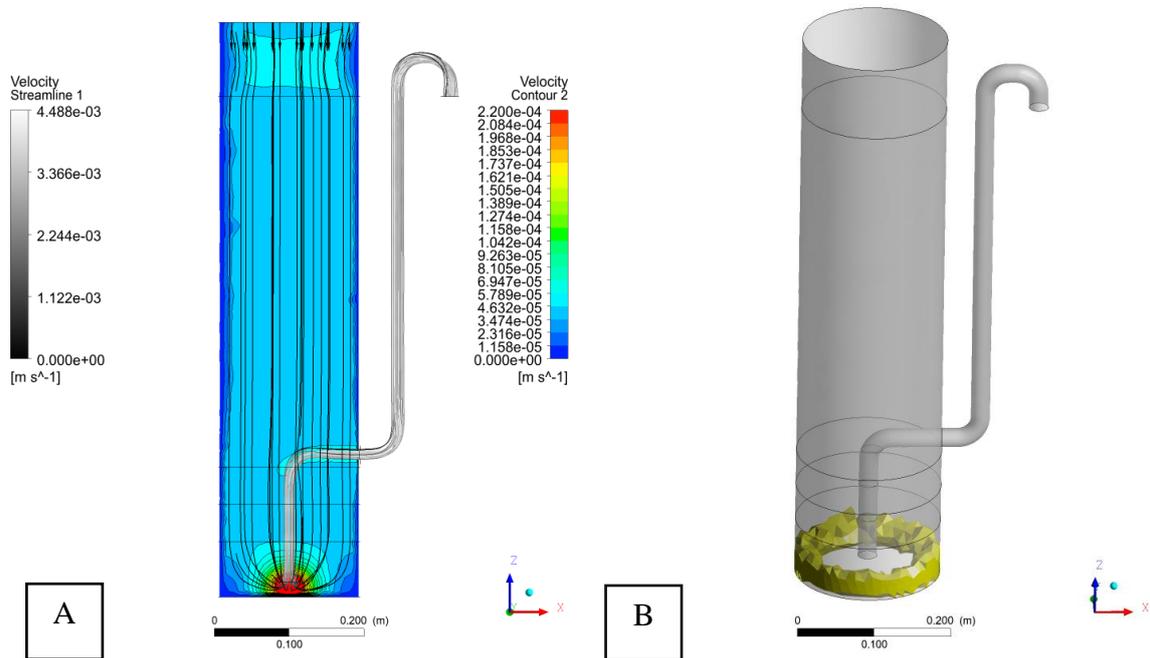
786

Dead zone volume in yellow).

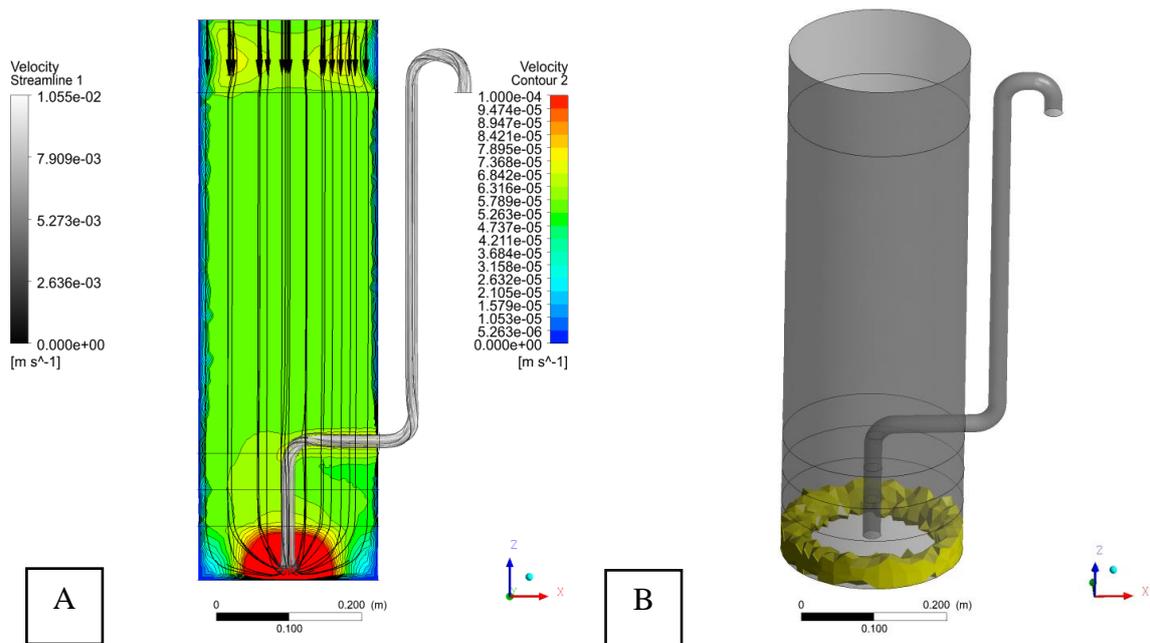
787



788 Figure S3 – Dead zone in C-HSSF2 (A - Current lines and velocity contour plane; B -  
 789 Dead zone volume in yellow).



790 Figure S4 – Dead zone in I-HSSF1 (A - Current lines and velocity contour plane; B -  
 791 Dead zone volume in yellow).



792 Figure S5 – Dead zone on I-HSSF2 (A - Current lines and velocity contour plane; B -  
 793 Dead zone volume in yellow).

794

795 **References**

796 ABNT NBR 6458. Grãos de pedregulho retidos na peneira de abertura 4,8 mm —  
 797 Determinação da massa específica, da massa específica aparente e da absorção de água.  
 798 [Gravel grains retained in the 4.8 mm opening sieve - Determination of specific gravity,  
 799 apparent specific gravity and water absorption]. Brazil. Rio de Janeiro, 2016.  
 800 Associação Brasileira de Normas Técnicas - ABNT.

801 ABNT NBR 6502. Rochas e solos. [Rocks and soils]. Brazil. Rio de Janeiro, 1995.  
 802 Associação Brasileira de Normas Técnicas - ABNT.

803 ABNT NBR 11799. Material filtrante — Areia, antracito e pedregulho —Especificação.  
 804 [Filter material - Sand, anthracite and gravel - Specification]. Brazil. Rio de Janeiro,  
 805 2016. Associação Brasileira de Normas Técnicas - ABNT.

806 ABNT NBR 13292. Solo – Determinação do coeficiente de permeabilidade de solos  
807 granulares à carga constante. [Determination of the permeability coefficient of granular  
808 soils at constant load]. Brazil. Rio de Janeiro, 1995. Associação Brasileira de Normas  
809 Técnicas - ABNT.

810 ABNT NM 45. Agregados – Determinação da massa unitária e do volume de vazios.  
811 [Aggregates - Determination of unit mass and void volume]. Brazil. Rio de Janeiro,  
812 2006. Associação Brasileira de Normas Técnicas - ABNT. Norma Mercosul – NM.

813 ABNT NM 248. Agregados – Determinação da composição granulométrica.  
814 [Aggregates - Determination of particle size composition]. Brazil. Rio de Janeiro, 2001.  
815 Associação Brasileira de Normas Técnicas - ABNT. Norma Mercosul – NM.